

Mark Scheme (Results)

January 2015

Pearson Edexcel International GCSE Mathematics B (4MB0) Paper 02

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# **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded.
   Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.
  - Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.
- Types of mark ∘M marks: method marks ∘A marks: accuracy marks
  - B marks: unconditional accuracy marks (independent of M marks)
- Abbreviations ocao correct answer only oft follow through oisw
   ignore subsequent working oSC special case
  - oe or equivalent (and appropriate)
  - dep dependent oindep independent oeeoo each error or omission

#### No working

If no working is shown then correct answers normally score full marks If no working is shown then incorrect (even though nearly correct) answers score no marks.

## With working

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

Any case of suspected misread loses A (and B) marks on that part, but can gain the M marks.

If working is crossed out and still legible, then it should be given any appropriate marks, as long as it has not been replaced by alternative work.

If there is a choice of methods shown, then no marks should be awarded, unless the answer on the answer line makes clear the method that has been used.

If there is no answer on the answer line then check the working for an obvious answer.

## Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: e.g. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eq algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

#### Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part ofthe question CANNOT be awarded in another.

	Question	Working	Answer	Mark	Notes
1.	(a)	365×24×60			M1
		30			
			17 520 sales	2	A1
	(b)	$\frac{"17520"}{120} \times 100$ (oe)			M1
		120	14 600 sales	2	A1
	(c)	$\frac{365 \times x \times 60}{"14600"} = 27 $ (oe)			M1
			x = 18 (cao)	2	A1
					Total 6 marks

Question	Working	Answer	Mark	Notes
2.				
	$0 < m \le 25$ : <b>FD=2.0</b> (1.0)(drawn)			B1
	Finding a scale factor eg 75/25  If <b>no working for scale factor seen</b> then seeing one of $70 < m \le 80$ : <b>FD=8.8</b> ( <b>4.4</b> ) (drawn)  or			M1
	80 $< m \le 100$ : <b>Freq. = 6</b> (entered in table) Seeing both			
	70 $< m \le 80$ : <b>FD=8.8</b> ( <b>4.4</b> ) (drawn) and			
	$80 < m \le 100$ : <b>Freq. = 6</b> (entered in table)			A1
	$\therefore 50 < m \le 70 : \mathbf{Freq.} = 70 \text{ (entered in table)}$			B1 ft on "6"
	∴ $50 < m \le 70$ <b>FD</b> = <b>7.0</b> ( <b>3.5</b> )(drawn) <b>NB:</b> ft on "Freq. 70"		5	B1 ft
				Total 5 marks

(	Question	Working	Answer	Mark	Notes
3.	(i)	3x(2x-5) - 6(x+2) (numerator, oe, allow 1 incorrect sign if expanded)			M1
		$(x + 2) (2x - 5)$ OR $2x^2 - x - 10$ (denominator)			B1
		$\frac{6x^2 - 21x - 12}{(x+2)(2x-5)}  \text{OR}  \frac{6x^2 - 21x - 12}{2x^2 - x - 10}$ OR			
		$\frac{3(2x+1)(x-4)}{(x+2)(2x-5)}$ (oe)		3	A1
	(ii)	" $6x^2 - 21x - 12$ " = 0 (oe) <b>NB:</b> must be from a fraction answer in (i)			M1
		3(2x + 1)(x- 4) (= 0) (solving "their" trinomial quadratic)			M1
			$x = -\frac{1}{2}$		A1
			x = 4	4	A1
					Total 7 marks

	Question	Working	Answer	Mark	Notes
4.	(a)	$a\times(-1)+b=1$ (oe)			B1
		$a\times4+b=16$		2	B1
		<b>NB:</b> order of award of Bs for ePEN			
	(b)	Rearranging so that coef of a or b is the same in			
		both equations			
		OR isolating a or b then adding or subtracting			
		equations			M1 ft on candidate's two linear
		OR substitute expressions for a or b to obtain b			simultaneous equations
		or a			
			a = 3 (cao)		A1
		<b>NB:</b> Note order of award of A1s for ePEN	b = 4 (cao)	3	A1
	(c)	" $y = 3x + 4$ " and rearranged or after			M1
		exchanging $x$ and $y$ (oe)			
			x-4		
			$1 : x \mapsto {3}$	2	A1 ft
			$f^{-1}:x\mapsto \frac{x-4}{3}$ $f^{-1}(x) = \frac{x-4}{3}$ (cao)		
	(d)	$3x + 4$ " = " $\frac{x-4}{3}$ "			M1
		<u> </u>	x = -2 (cao)	2	A1
					Total 9 marks

	Question	Working	Answer	Mark	Notes
5.	(a)	15 is the number of people in the survey who do not enjoy any of the three activities (oe) OR symbolic representation eg n $(L \cup R \cup W)'$ = 15 (oe)		1	B1
	(b)	20 x 4 4 15		2	B2 (-1 eeoo)
	(c)	100 = "15 + x + x + 20 + 7 + 25 + 4 + 9"			M1
			x = 10 (cao)	2	A1

(d)(i)	46		B1 ft
(d)(ii)	23		B1 ft
(d)(iii)	25	3	B1 cao
			Total 8 marks

Question	Working	Answer	Mark	Notes
6. (a)	$x = \sqrt{5^2 - 4^2}$			M1
		x = AD = 3	2	A1
(b)	$\frac{1}{2}(4+2x)(x+y) = 10 \times \left(\frac{1}{2} \times 4 \times x\right)  \text{(oe)}$			M1
	$\therefore \frac{1}{2} (4 + 2 \times "3") ("3" + y) = 10 \times \left( \frac{1}{2} \times 4 \times "3" \right)$			M1 DEP (Substitution for $x$ )
	$\therefore DC = \cancel{y}  \frac{60-15}{5}$			M1 DEP (isolated y)
		y = DC = 9	4	A1
(c)	$EBCD = 10$ " $\triangle AED$ " $(=\triangle ABC) - ``\triangle AED$ " (oe)			M1
		EBCD = 54	2	A1
				Total 8 marks

Question	Wor	king	Answer	Mark	Notes
7. (a)	First book	Second book  Textbook	Allswer	Wark	Notes
	$\frac{30}{50}$ Textbook $\left(\frac{20}{50}\right)$ Novel	$\left(\frac{20}{49}\right)$ Novel $\left(\frac{30}{49}\right)$ Textbook			
		$\left(\frac{19}{49}\right)$ Novel	Start deducting errors starting with the last B box in ePEN	3	B1, B1, , B1 (each pair)

(b)	$\frac{30}{50} \times "\frac{29}{49}"$				
	50 49				
	OR Complement				
	$1 - "\left(\frac{20}{50} \times \frac{19}{49}\right)" - "\left(\frac{20}{50} \times \frac{30}{49}\right)" - \left(\frac{30}{50} \times "\frac{20}{49}"\right)$			M1	
		$\frac{870}{2450}$ (o.e), awrt (0.355), 35.5%	2	A1	
(c)	55 and 54 (eg 55x54) used as denominators in a probability product			M1	
	$1 - 30 \times 29$ $55  54$				
	OR				
	$\frac{25}{55} \times \frac{24}{54} + \frac{25}{55} \times \frac{30}{54} + \frac{30}{55} \times \frac{25}{54}$			M1	DEP
		2100/2970, 210/99, awrt(0.707) , 70.7%	3	A1	
					Total 8 marks

Question	Working	Answer	Mark		Notes
	Penalise labelling or no labelling ONCE only				
<b>8.</b> (a)	A drawn and labelled		1	B1	
(b)		B = (-1, 0) $(-3, 0)$ $(1, -2)$	2	B2	(-1 each incorrect coordinate pair) Accept column vectors and embedded coordinates in 2x3 matrices
(c)	B drawn and labelled		1	B1	ft on seen coordinates
(d)		(-1, -2) (-3, -6) (-1, -6)	2	В2	ft (-1 each incorrect coordinate pair) Accept column vectors and embedded coordinates in 2x3 matrices
(e)	C drawn and labelled		1	B1	ft on seen coordinates
(f)	Reflection in $y = -x$ NB: SC: $\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$ seen on its own and no explanation scores P1 P0		2	B1 B1	
	explanation scores B1 B0				Total 9 marks

Question	Working	Answer	Mark	Notes
	Penalise ncc ONCE only			
	in this question			
<b>9.</b> (a)	$\cos 15 = \frac{11}{OA}$			M1
	OA			
		<i>OA</i> = 11.388-> <b>11.4</b>	2	A1
(b)	$\tan 15 = \frac{OB}{11}  (OB = 2.947)$			M1
	∴ <i>AP</i> = "11.388"−"2.947"			M1
	OR			
	$11^2 = AP \times ("11.388" + "2.947")$			(M1)
		<i>AP</i> = 8.441-> <b>8.44</b>	3	A1
(c)	$BC^2 = "2.947"^2 + "2.947"^2 - 2 \times "2.947" \times "2.947" \times \cos(\angle BOC = 105)$	711 = 0.441 × 0.44		M1
	$BC = \sqrt{"21.865"}$ (= 4.676)			M1 DEP
	OR			
	(AC = "8.441" + "2.947" + "2.947" = 14.335)			(M1)
	$BC^2 = "14.335"^2 + 11^2 - 2 \times "14.335" \times 11 \times \cos 15$			
	$BC = \sqrt{21.868} \ (=14.676)$			(M1 DEP)
	<b>OR</b> $(\angle OCB = 37.5)$			
	$\frac{11}{\sin"37.5"} = \frac{BC}{\sin 15}$			(M1)
	$BC = \frac{11 \times \sin 15}{\sin"37.5"}$			(M1 DEP)
	<b>OR</b> $(\Delta BOC \text{ is isos. } \Delta)$			
	$\angle OBC = \frac{180 - (180 - 75)}{2} $ (=37.5)			(M1)

	$BC = 2 \times "2.947" \times \cos"37.5"$		(M1	DEP)
		BC = 4.676, 4.677->4.68	3 A1	
(d)	$(BCPQ = \Delta ABC - \Delta APQ \text{ method})$ :		M1	
	$PQ = "8.441" \times \tan 15 \ (= 2.2618)$			
	$\Delta APQ = \frac{1}{2} \times "8.441" \times "2.2618" \ (=9.5459)$		M1	DEP
	$\Delta ABC = \frac{1}{2} \times 11 \times ("8.441" + 2 \times "2.947") \times \sin 15 \ (= 20.406)$		M1	
	$BCPQ = \Delta ABC - \Delta APQ$		M1	DEP
		BCPQ = 10.86 -> 10.9 cm <sup>2</sup>	A1	
	<b>OR</b> $(BCPQ = \Delta BCP + \Delta BPQ \text{ method})$			
	$PQ = "8.441" \times \tan 15 \ (= 2.2618)$		(M1)	)
	$PB^{2} = 2.947^{2} + 2.947^{2} - 2 \times 2.947 \times 2.947 \times \cos 75$ $\therefore PB = 3.588$			
	$\Delta BPQ = \frac{1}{2} \times "2.2618" \times "3.588" \times \sin 37.5  (= 2.470)$		(M1	DEP)
	$\Delta BCP = \frac{1}{2} \times "4.677" \times (2 \times "2.947") \times \sin 37.5 \ (= 8.3906)$		(M1)	)
	$BCPQ = \Delta BCP + \Delta BPQ$		(M1	DEP)
		BCPQ = 10.86 -> 10.9 cm <sup>2</sup>	(A1)	)
	<b>OR</b> $(BCPQ = \Delta OCB + \Delta OPB + \Delta BPQ \text{ method})$			
	$PQ = "8.441" \times \tan 15 \ (= 2.2618)$		(M1)	)

$(PB^2 = 2.947^2 + 2.947^2 - 2 \times 2.947 \times 2.947 \times \cos 75)$ \therefore PB = 3.588			
$\Delta BPQ = \frac{1}{2} \times "2.2618" \times "3.588" \times \sin 37.5  (= 2.470)$			(M1 DEP)
$\Delta OCB + \Delta OPB = \frac{1}{2} \times "2.947" \times "2.947" \times \sin 105$			(M1)
$+\frac{1}{2}$ × "2.947" × "2.947" × sin 75			
(=4.1944 + 4.1944)			
$BCPQ = \Delta OCB + \Delta OPB + \Delta BPQ$			(M1 DEP)
	$BCPQ = 10.9 \text{ cm}^2$	5	(A1)
			Total 13 marks

Question	Working	Answer	Mark	Notes
<b>10.</b> (a)	Penalise ncc ONCE only in this question $V = lh^2 - 2 \times \left(\frac{1}{2} \times \frac{4}{3} \pi \left(\frac{h}{2}\right)^3\right) $ (3 correct volumes)			M1
		$V = h^2 \left( l - \frac{\pi h}{6} \right) $ (oe)	2	A1
(b)	$V = "(10-h)h^2 - \frac{4}{3}\pi \left(\frac{h}{2}\right)^3$ " (substitution for <i>l</i> )			M1
		(cc)	2	A1
(c)		8.5, 48.9, 59.5 or 59.6	3	B1 B1 B1
(d)	<b>NB:</b> Accuracy for both plotting and	Curve drawn	3	B3 (-1 eeoo)  -1 mark  for:     straight line segments,     each point missed,     each missed segment,     each point not plotted,     each point incorrectly     plotted,     tramlines,

	drawing is $\pm \frac{1}{2} ss$				very poor curve
(e)	If using calculus, accept 64 only	V = 64	1	B1	ft
(f)	V = 60 line drawn			M1	
	OR inferred from values for h				
	OR from intersection of vertical line				
	from x-axis with c's curve at $V = 60$				
	OR seeing one of 3.7 or 5 (ft)				
	Allow "x" for h	$h > 3.7 \ (+/- \text{grid ss} = \pm 0.1)$		A1	ft
		$h \le 5.0$ (or better)		A1	ft
		$(+/- \text{grid ss} = \pm 0.1)$			
	<b>NB:</b> If the values "3.7" and/ or "5"	Accept weak inequalities or			
	- ·	equalities			
	inequality but appear in $l + h = 10$ (eg				
	l + "3.7" = 10) award the A1 ft for				
	each occurrence (ie of "3.7" and "5")				
		leading to <i>l</i> < 6.3		A1	ft
		<i>l</i> >5.0 (accept "5")	5	A1	ft Note that 5.0 < l < 6.3 scores A1ft A1ft
		Accept weak inequalities for l			
		<b>NB:</b> "5.0" < <i>l</i> < "6.3" with no			Total 16 marks
		working scores full marks.			1

Questio	n Working	Answer	Mark	Notes
<b>11.</b> (a)(i)		$\overrightarrow{AB} = 2\mathbf{b} - \mathbf{a}$		B1
(a)(ii)		$\overrightarrow{OQ} = 2\mathbf{b} + k\mathbf{a}$	2	B1
(b)		$\overrightarrow{AP} = \frac{1}{3}(\text{"2b} - \mathbf{a}\text{"})$	1	B1 ft
(c)(i)	$\overrightarrow{OA} = \overrightarrow{OP} + \overrightarrow{PA}$ $= \frac{1}{\mu} (\text{"2b} + k\mathbf{a}\text{"}) + \text{"} - \frac{1}{3} (2\mathbf{b} - \mathbf{a})\text{"} $ (oe) $\overrightarrow{OR}$ $\overrightarrow{OA} = \overrightarrow{OQ} + \overrightarrow{QB} + \overrightarrow{BA}$ $= \frac{2}{3} \mu (\mathbf{a} + \mathbf{b}) - k\mathbf{a} - (2\mathbf{b} - \mathbf{a})$ (oe)			B1 ft
(c)(ii)	$\overrightarrow{OA} = \left(\frac{k}{\mu} + \frac{1}{3}\right)\mathbf{a} + \left(\frac{2}{\mu} - \frac{2}{3}\right)\mathbf{b}  = \mathbf{a}  \text{(oe)}$ $\overrightarrow{OR}$ $\overrightarrow{OA} = \frac{2}{3}\mu(\mathbf{a} + \mathbf{b}) - k\mathbf{a} - (2\mathbf{b} - \mathbf{a}) = \mathbf{a}  \text{(oe)}$			M1
	comp of <b>b</b> : $0 = \left(\frac{2}{\mu} - \frac{2}{3}\right)$ OR $\frac{2}{3}\mu = 2$			M1 DEP

		$\therefore \mu = 3$		A1
	comp of <b>a</b> : $1 = \left(\frac{k}{\mu} + \frac{1}{3}\right)$ OR $1 = \frac{2}{3}\mu - k + 1$			M1 DEP
		$\therefore k = 2$	6	A1
(d)				M1
		$\Delta OPA = 3 \text{ (cm}^2)$	2	A1
				Total 11 marks

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